

p5

When you use the Ratio test to find the interval of convergence, what are the 3 possible answers for the limit & what do they mean?

$$\text{Ratio test } R = \lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right|$$

$$1. \infty \quad R = 0 \quad I = \{c\}$$

$$2. 0 \quad R = \infty \quad I = (-\infty, \infty)$$

$$3. \# \quad R = \frac{1}{2} I \quad I = \text{solve for}$$

p6

Find the Radius of convergence & the interval of convergence for

$$\sum_{n=1}^{\infty} \frac{x^n}{n!}$$

$$\sum_{n=1}^{\infty} \frac{x^n}{n!} \quad R = \lim_{n \rightarrow \infty} \left| \frac{x^{n+1}}{(n+1)!} \cdot \frac{n!}{x^n} \right|$$

$$R = \lim_{n \rightarrow \infty} \left| \frac{x^n \cdot x \cdot n!}{x^n (n+1) (n!)} \right|$$

$$R = \lim_{n \rightarrow \infty} \left| \frac{x}{n+1} \right|$$

$$R = |x| \lim_{n \rightarrow \infty} \left| \frac{1}{n+1} \right|$$

$$R = |x| (0) < 1 \quad \text{Always}$$

$$\text{Interval: } (-\infty, \infty)$$

$$\text{Radius: } \infty$$

p7

Find the Radius & Interval of convergence for

$$\sum_{n=1}^{\infty} n! (2x+1)^n$$

$$\sum_{n=1}^{\infty} n! (2x+1)^n \quad R = \lim_{n \rightarrow \infty} \left| \frac{(n+1)! (2x+1)^{n+1}}{n! (2x+1)^n} \right|$$

$$R = \lim_{n \rightarrow \infty} \left| \frac{(n+1) n! (2x+1)^n (2x+1)}{n! (2x+1)^n} \right|$$

$$R = |2x+1| \lim_{n \rightarrow \infty} |n+1|$$

$$R = |2x+1| (\infty) < 1$$

$$\text{when } 2x+1=0$$

$$x = -\frac{1}{2}$$

$$\text{Interval: } \left\{ -\frac{1}{2} \right\}$$

$$\text{Radius: } 0$$

P8

Find the
Radius & Interval
of convergence for

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{n} (x-5)^n$$

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{n} (x-5)^n \quad R = \lim_{n \rightarrow \infty} \left| \frac{(x-5)^{n+1}}{n+1} \cdot \frac{n}{(x-5)^n} \right|$$

$$\text{Radius} \quad R = \lim_{n \rightarrow \infty} \left| \frac{(x-5)^n (x-5)^1 n}{(x-5)^n (n+1)} \right|$$

$$\text{Interval} \quad R = |x-5| \lim_{n \rightarrow \infty} \left| \frac{n}{n+1} \right|$$

$$\text{check 4!} \quad R = |x-5| (1) < 1 \quad |x-5| < 1 \text{ and } x-5 > -1$$

$$\text{check 6} \quad \sum_{n=1}^{\infty} \frac{(-1)^n (6-5)^n}{n} = \sum_{n=1}^{\infty} \frac{(-1)^n (1)^n}{n} = \sum_{n=1}^{\infty} \frac{(-1)^n}{n}$$

converges by alternating $\frac{1}{n}$ is decreasing & $\lim_{n \rightarrow \infty} \frac{1}{n} = 0$.

$x < 6$ and $x > 4$
diverges by p series $p=1 \neq 1$.