

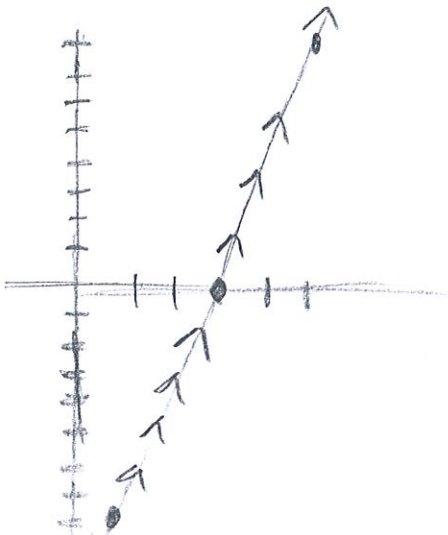
Supplement: Graphing and Rewriting Parametric

1-3: Express in the form of $y=f(x)$ by eliminating the parameter and graph each.

1. $x = t + 3, y = 4t$

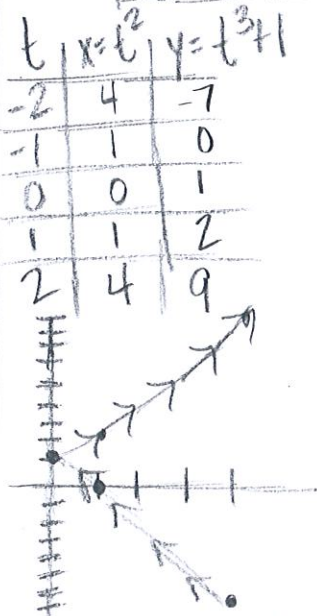
t	$x = t + 3$	$y = 4t$
-2	1	-8
0	3	0
2	5	8

$t = x - 3$
 $y = 4(x - 3)$
 $y = 4x - 12$



2. $x = t^2, y = t^3 + 1$

$t = \sqrt{x}$
 $y = (\sqrt{x})^3 + 1$
 $y = x^{3/2} + 1$



3. $x = \ln t, y = 2 - t$

$t = e^x$
 $y = 2 - e^x$

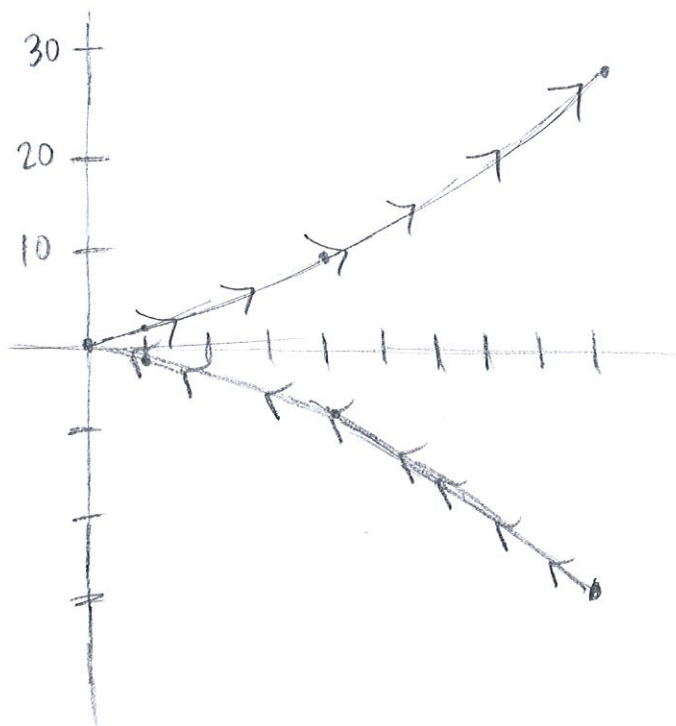
$t > 0$

t	$x = \ln t$	$y = 2 - t$
1/4	-1.4	1.75
1/2	-0.7	1.5
1	0	1
3	1.1	-1



4. Graph the curve and draw an arrow specifying the direction of motion for $x = t^2, y = t^3$

t	$x = t^2$	$y = t^3$
-3	9	-27
-2	4	-8
-1	1	-1
0	0	0
1	1	1
2	4	8
3	9	27



5-8: Find Parametric Equations for the given curve

circle: center $(-9, 4)$ $R=7$

5. $4x - y^5 = 5$

$4x = 5 + y^5$

$x = \frac{5}{4} + \frac{1}{4}y^5$

$c(t) = \left(\frac{5}{4} + \frac{1}{4}t^5, t \right)$

6. $(x+9)^2 + (y-4)^2 = 49$

$c(t) = (-9 + 7\cos t, 4 + 7\sin t)$

7. Line through $(2, 5)$ Perpendicular to $y=3x$

$m = -\frac{1}{3}$

$c(t) = (2+t, 5 - \frac{1}{3}t)$

8. $\left(\frac{x}{4}\right)^2 + \left(\frac{y}{9}\right)^2 = 1$

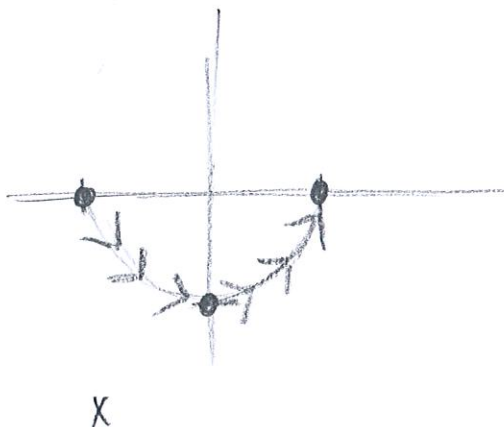
$c(t) = (4\cos t, 9\sin t)$

9. Find an interval of t values such that $c(t) = (\cos t, \sin t)$ traces the lower half of the unit circle.

$\pi \leq t \leq 2\pi$

$-\pi \leq t \leq 0$

t	$x = \cos t$	$y = \sin t$
π	-1	0
$\frac{3\pi}{2}$	0	-1
2π	1	0

10. Find an interval of t -values such that $c(t) = (2t+1, 4t-5)$ parametrizes the segment from $(-7, -7)$ to $(7, 7)$.

$$2t+1=0 \quad \text{OR} \quad 4t-5=-7$$

$$t = -\frac{1}{2} \quad \quad 4t = -2$$

$$t = -\frac{1}{2}$$

$$2t+1=7 \quad \text{OR} \quad 4t-5=7$$

$$2t=6 \quad \quad 4t=12$$

$$t=3 \quad \quad t=3$$

$-\frac{1}{2} \leq t \leq 3$