

Year	White	African American	Asian	Hispanic	American Indian	Pacific Islander	Two or More Races	Not Specified	$t$	Total
2007	682	391	31	43	1	n/a	n/a	22	0	1170
2008	978	584	54	92	3	n/a	n/a	43	1	1754
2009	1117	562	55	92	4	n/a	n/a	42	2	1872
2010	1241	624	64	111	4	0	0	0	3	2044
2011	1259	620	52	119	3	0	21	0	4	2074
2012	1257	608	47	109	3	0	27	0	5	2051
2013	1296	627	46	132	1	0	37	0	6	2139
2014	1288	649	47	137	1	1	54	0	7	2177
2015	1272	734	57	168	2	1	67	0	8	2301
2016	1267	803	53	192	1	1	87	0	9	2404
2017	1226	865	67	216	2	1	89	0	10	2466
2018	1201	853	73	234	4	0	100	0	11	2465

Data source: National Center for Education Statistics, U.S. Dept of Education.

**Enter Data into your TI-84**

1. Press (STAT)
2. Press 5: SetUpEditor Press Enter
3. Press (STAT)
4. Press 1: Edit
5.  $L_1 = 0, 1, \dots, 11$  for the years
6.  $L_2 = 1170, 1754, \dots$  for the Total Population of Hillgrove
7. Press 2<sup>nd</sup> Quit (to go to Homescreen)

**Exponential**

1. Press (STAT)
  2. CALC
  3. 0: ExpReg
  4. Enter: 5 times
- $y = a \cdot b^x$   
 $a = 1565$   
 $b = 1.0494$   
 $r^2 = .72$   
 $y = (1565)(1.0494)^x$

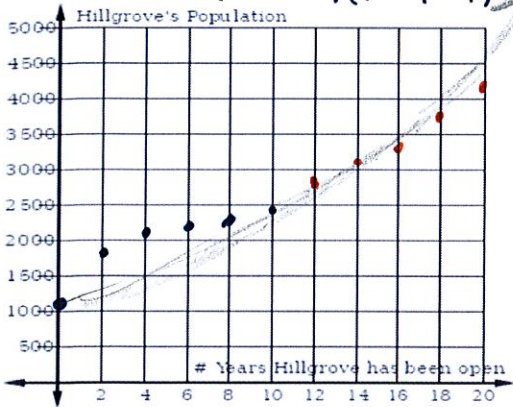
**Logistic**

1. Press (STAT)
  2. CALC
  3. B: Logistic
  4. Enter: 5 times
- $y = c / (1 + a e^{(-bx)})$   
 $a = .7708$   
 $b = .40956$   
 $c = 2397$   
 $r^2 = .92$   
 $y = \frac{2398}{1 + .7708 e^{-.40956x}}$

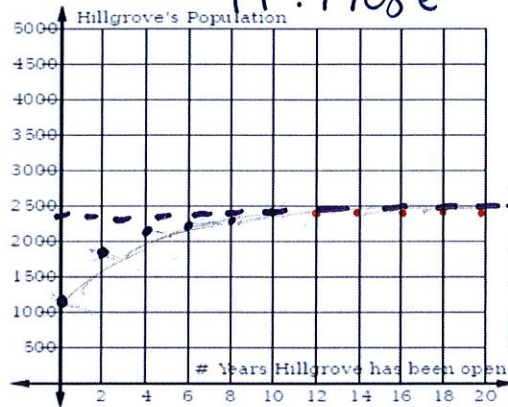


Graph the Exponential and Logistic equations: plug the equations into the calculator to predict the population in future years.

Exponential  $y = (1565)(1.0494)^x$



Logistic:  $y = \frac{2398}{1 + .7708 e^{-.40956x}}$



HA: Carrying Capacity

What is the prediction of the population in 14, 18, and 20 years?

Exponential:	$y(12)$	$y(14)$	$y(16)$	$y(18)$	$y(20)$
	2791	3073	3385	3727	4105
Logistic:	2385	2392	2395	2396	2397

Which model is a better model for Hillgrove's population? Why?

Logistic: because can not grow exponentially forever.

<https://www.geogebra.org/m/Pd4Hn4BR>

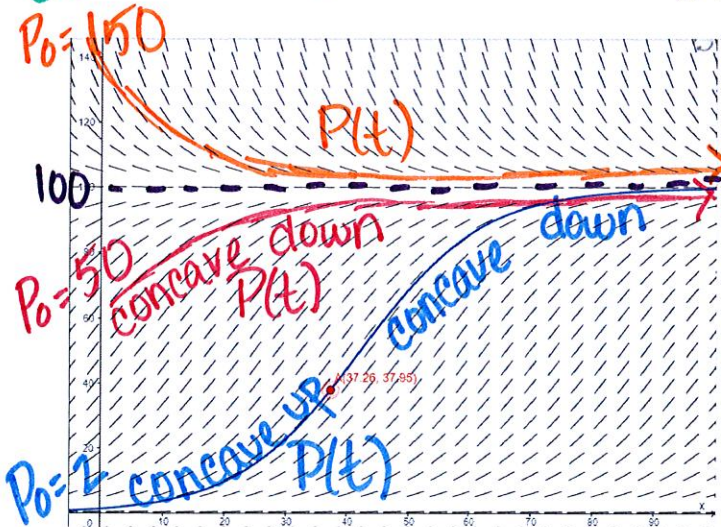
$\frac{dP}{dt} = .1P - .001P^2$  "Force One"

$\frac{dP}{dt} = .1P \left[ \frac{.1P}{.1P} - \frac{.001P^2}{.1P} \right]$

$\frac{.001}{.1} = \frac{1}{100}$

$\frac{dP}{dt} = KP \left[ 1 - \frac{P}{A} \right]$

$\frac{dP}{dt} = .1P \left[ 1 - \frac{P}{100} \right]$



What is the carrying capacity?  $A = 100$

What is the growth rate?  $K = .1$

What would your graph look like if you started over the carrying capacity? **concave up**

If you lie **above** the carrying capacity your graph is **decreasing** with **negative** slopes

If you lie **below** the carrying capacity your graph is **increasing** with **positive** slopes

What is the concavity?