

Additional  
Integration 1

$$\int_0^{\frac{\pi}{2}} \sin^3 x \, dx$$

$$\int_0^{\frac{\pi}{2}} \sin^3 x \, dx \quad (\text{Odd } \smile \text{ Rewrite } \smile \text{ with singleton } \smile)$$

$$\int_0^{\frac{\pi}{2}} \sin x \cdot \sin^2 x \, dx \quad (\text{Rewrite non-singleton terms in other trig function})$$

$$= \int_0^{\frac{\pi}{2}} -\sin x (1 - \cos^2 x) \, dx \quad (\text{Use } u\text{-Substitution})$$

$$= \int_0^1 (1 - u^2) \, du$$

$$\int_0^1 (1 - u^2) \, du$$

$$u - \frac{u^3}{3} \Big|_0^1 = \left(1 - \frac{1}{3}\right) - (0 - 0) = \boxed{\frac{2}{3}}$$

$$u = \cos x$$
$$du = -\sin x \, dx$$
$$u\left(\frac{\pi}{2}\right) = \cos\frac{\pi}{2} = 0$$
$$u(0) = \cos(0) = 1$$

Additional  
Integration 2

$$\int \cos^2 x \, dx$$

$$\int \cos^2 x \, dx \quad (\text{Even so use } \cos^2 x = \frac{1}{2}[1 + \cos(2x)]$$
$$\sin^2 x = \frac{1}{2}[1 - \cos(2x)]$$

$$\int \frac{1}{2}[1 + \cos(2x)] \, dx$$

$$\frac{1}{2} \int [1 + \cos(2x)] \, dx$$

$$\frac{1}{2} \left[ x + \frac{\sin(2x)}{2} \right] + C$$

$$\frac{1}{2}x + \frac{1}{4}\sin(2x) + C$$