

What are the four steps to making a graph from its Limits?

1. Label each piece

✓ Vertical Asymptotes:

$$\lim_{x \rightarrow c^+} f(x) \text{ or } \lim_{x \rightarrow c^-} f(x) \text{ or } \lim_{x \rightarrow c} f(x) = \pm\infty$$

✓ Horizontal Asymptotes: $\lim_{x \rightarrow \pm\infty} f(x) = L$

✓ Open Circles: $\lim_{x \rightarrow c} f(x) = L$

✓ Closed Circles: $f(x) = y$

2. Graph VA, HA, Open, & Closed Circles

3. Graph behavior at VA & Open Circles

4. Graph end behavior

Sketch the graph of a function with the following Limits:

$$\lim_{x \rightarrow -2^-} f(x) = \infty$$

$$\lim_{x \rightarrow \infty} f(x) = -\infty$$

$$\lim_{x \rightarrow -2^+} f(x) = -\infty$$

$$\lim_{x \rightarrow -\infty} f(x) = -\infty$$

$$f(2) = 3$$

$$\lim_{x \rightarrow 2} f(x) = -3$$

$$\lim_{x \rightarrow -2} f(x) = \infty \quad \left. \begin{array}{l} \lim_{x \rightarrow -2^-} f(x) = \infty \\ \lim_{x \rightarrow -2^+} f(x) = -\infty \end{array} \right\} \text{VA: } x = -2$$

$$\lim_{x \rightarrow -2^+} f(x) = -\infty$$

$$f(2) = 3 \text{ closed circle } (2, 3)$$

$$\lim_{x \rightarrow \infty} f(x) = -\infty \text{ EB (Right, down)}$$

$$\lim_{x \rightarrow -\infty} f(x) = -\infty \text{ EB (Left, down)}$$

$$\lim_{x \rightarrow 2} f(x) = -3 \text{ open circle } (2, -3)$$

