

$$\frac{d}{dx} [f(g(x))] =$$

$$\frac{d}{dx} [f(AT)] =$$

$$\frac{d}{dx} [f(g(x))] = f'(g(x)) \cdot \frac{d}{dx} (g(x))$$

$$\frac{d}{dx} [f(AT)] = f'(AT) \cdot \frac{d}{dx} (AT)$$

▣ The derivative of the outside times the derivative of the inside.

$$f(x) = g(\sqrt[3]{x}) + 3x^4$$

Find
 $f'(x)$

$$f(x) = g(\sqrt[3]{x}) + 3x^4$$

$$f'(x) = g'(\sqrt[3]{x}) \cdot \frac{d}{dx} [x^{1/3}] + 12x^3$$

$$f'(x) = g'(\sqrt[3]{x}) \cdot \frac{1}{3} x^{-2/3} + 12x^3$$

$$f'(x) = \frac{g'(\sqrt[3]{x})}{3x^{2/3}} + 12x^3 = \frac{g'(\sqrt[3]{x})}{3(\sqrt[3]{x})^2} + 12x^3$$

▣ Remember: $\frac{d}{dx} [g(AT)] = g'(AT) \cdot \frac{d}{dx} [AT]$

$$f(x) = \sin(\sqrt{x})$$

Find $f'(x)$

$$f(x) = \sin(\sqrt{x}) \quad \text{Find } f'(x)$$

$$f(x) = \sin(x^{1/2})$$

$$f'(x) = \cos(x^{1/2}) \cdot \frac{d}{dx} [x^{1/2}]$$

$$f'(x) = \cos(\sqrt{x}) \cdot \frac{1}{2} x^{-1/2}$$

$$f'(x) = \frac{\cos \sqrt{x}}{2\sqrt{x}}$$

Remember $\frac{d}{dx} [\sin(AT)] = \cos(AT) \cdot \frac{d}{dx} [AT]$

$$f(x) = \cos(e^{3x})$$

Find $f'(x)$

$$f(x) = \cos(e^{3x}) \quad \text{Find } f'(x)$$

$$f'(x) = -\sin(e^{3x}) \cdot \frac{d}{dx} [e^{3x}]$$

$$f'(x) = -\sin(e^{3x}) \cdot e^{3x} \cdot \frac{d}{dx} [3x]$$

$$f'(x) = -\sin(e^{3x}) \cdot e^{3x} \cdot 3$$

$$f'(x) = -3\sin(e^{3x}) \cdot e^{3x}$$

Remember $\frac{d}{dx} [\cos(AT)] = -\sin(AT) \cdot \frac{d}{dx} [AT]$

$$\begin{aligned} \frac{d}{dx} [e^{AT}] &= e^{AT} \cdot \frac{d}{dx} [AT] \end{aligned}$$

$$f(x) = \tan(2x+3)$$

Find $f'(x)$

$$f(x) = \tan(2x+3) \quad \text{Find } f'(x)$$

$$f'(x) = \sec^2(2x+3) \cdot \frac{d}{dx} [2x+3]$$

$$f'(x) = \sec^2(2x+3) [2]$$

$$f'(x) = 2\sec^2(2x+3)$$

Remember $\frac{d}{dx} [\tan(AT)] = \sec^2(AT) \cdot \frac{d}{dx} [AT]$

$$f(x) = \cot(\sin x)$$

Find $f'(x)$

$$f(x) = \cot(\sin x) \quad \text{Find } f'(x)$$

$$f'(x) = -\csc^2(\sin x) \cdot \frac{d}{dx}[\sin x]$$

$$f'(x) = -\csc^2(\sin x) \cdot \cos x$$

$$f'(x) = -\cos x \csc^2(\sin x)$$

$$\blacksquare \text{ Remember } \frac{d}{dx}[\cot(AT)] = -\csc^2(AT) \cdot \frac{d}{dx}(AT)$$

$$f(x) = \sec(\pi x)$$

Find $f'(x)$

$$f(x) = \sec(\pi x) \quad \text{Find } f'(x)$$

$$f'(x) = \sec(\pi x) \tan(\pi x) \cdot \frac{d}{dx}[\pi x]$$

$$f'(x) = \sec(\pi x) \tan(\pi x) [\pi]$$

$$f'(x) = \pi \sec(\pi x) \tan(\pi x)$$

$$\blacksquare \text{ Remember } \frac{d}{dx}[\sec(AT)] = \sec(AT) \tan(AT) \cdot \frac{d}{dx}(AT)$$

$$f(x) = \csc(\sqrt{5x})$$

Find $f'(x)$

$$f(x) = \csc(\sqrt{5x}) \quad \text{Find } f'(x)$$

$$f(x) = \csc[(5x)^{1/2}]$$

$$f'(x) = -\csc(\sqrt{5x}) \cot(\sqrt{5x}) \cdot \frac{d}{dx}[(5x)^{1/2}]$$

$$f'(x) = -\csc(\sqrt{5x}) \cot(\sqrt{5x}) \cdot \frac{1}{2}(5x)^{-1/2} \cdot \frac{d}{dx}[5x]$$

$$f'(x) = -\csc(\sqrt{5x}) \cot(\sqrt{5x}) \cdot \frac{1}{2} \cdot \frac{1}{\sqrt{5x}} \cdot 5$$

$$f'(x) = \frac{-5 \csc(\sqrt{5x}) \cot(\sqrt{5x})}{2\sqrt{5x}}$$

$$\blacksquare \text{ Remember: } \frac{d}{dx}[\csc(AT)] = -\csc(AT) \cot(AT) \cdot \frac{d}{dx}(AT)$$