

What is the Product Rule for finding a derivative?

$$\text{Let } y = f(x) \cdot g(x)$$

$$y' = f(x) \cdot g'(x) + g(x) \cdot f'(x)$$

$$y' = (\text{first}) \frac{d}{dx} (\text{second}) + (\text{second}) \frac{d}{dx} (\text{first})$$

Find:  $f'(x)$

Given:  $f(x) = x^2 e^x$

$$f(x) = x^2 \cdot e^x$$

$$f'(x) = x^2 \frac{d}{dx} [e^x] + e^x \frac{d}{dx} [x^2]$$

$$f'(x) = x^2 \cdot e^x + e^x \cdot 2x$$

$$f'(x) = x e^x (x + 2)$$

What is the Quotient Rule for finding a derivative?

$$\text{Let } y = \frac{f(x)}{g(x)}$$

$$y' = \frac{g(x) f'(x) - f(x) g'(x)}{[g(x)]^2}$$

$$y' = \frac{lo d hi - hi d lo}{lo^2}$$

Find  $f'(x)$

Given:  $f(x) = \frac{2x+3}{x^2-x}$

$f(x) = \frac{2x+3}{x^2-x}$  hi

$x^2-x$  lo

$$f'(x) = \frac{(x^2-x) \frac{d}{dx}[2x+3] - (2x+3) \frac{d}{dx}[x^2-x]}{[x^2-x]^2}$$

$$f'(x) = \frac{(x^2-x)(2) - (2x+3)(2x-1)}{[x^2-x]^2}$$

• distribute negative!

$$f'(x) = \frac{2x^2 - 2x - (4x^2 - 2x + 6x - 3)}{(x^2-x)^2} = \frac{-2x^2 - 6x + 3}{(x^2-x)^2}$$