AP Calculus	Name
Area, Volume, & Avg. Value: Multiple Choice	DatePdDay 10
1. What is the area enclosed by the curves $y = x^3 - 8x^2 + 18x - 5$ and $y = x + 5$ ? (Calculator) (A) 10.667 (B) 11.833 (C) 14.583 (D) 21.333 (E) 32	2. What is the average value of $y = \frac{cosx}{x^2+x+2}$ on the closed interval [-1,3]? (Calculator) (A) -0.085 (B) 0.090 (C) 0.183 (D) 0.244 (E) 0.732
3. The base of a solid is the region in the first quadrant bounded by the $y$ -axis, the graph of $y = tan^{-1}x$ , the horizontal line $y = 3$ , and the vertical line $x = 1$ . For this solid, each cross section perpendicular to the $x - axis$ is a square. What is the volume of the solid? (Calculator) (A) 2.561 (B) 6.612 (C) 8.046 (D) 8.755 (E) 20.773	4. If $0 \le k < \frac{\pi}{2}$ and the area under the curve $y = cosx$ from $x = k$ to $x = \frac{\pi}{2}$ is 0.1, then k = (Calculator) (A) 1.471 (B) 1.414 (C) 1.277 (D) 1.120 (E) 0.436
5. If the region enclosed by the $y$ -axis, the line $y = 2$ , and the curve $y = \sqrt{x}$ is revolved about the $y$ -axis, the volume of the solid generated is (Non-Calculator) (A) $\frac{32\pi}{5}$ (B) $\frac{16\pi}{3}$ (C) $\frac{16\pi}{5}$ (D) $\frac{8\pi}{3}$	6. The average value of $cosx$ on the interval $\begin{bmatrix} -3,5 \end{bmatrix}$ is <b>(Non-Calculator)</b> (A) $\underline{sin5 - sin3}$ (B) $\underline{sin5 - sin3}$ (C) $\underline{sin3 - sin5}$ (D) $\underline{sin3 + sin5}$ (E) $\underline{\frac{sin3 + sin5}{8}}$
(E) $\pi$ 7. What is the area of the region in the first quadrant enclosed by the graphs of $y =$ cosx, $y = x$ , and the $y$ –axis? (Calculator) (A) 0.127 (B) 0.385 (C) 0.400 (D) 0.600 (E) 0.947	8. The base of a solid <i>S</i> is the region enclosed by the graph of $y = \sqrt{lnx}$ , the line $x = e$ , and the <i>x</i> —axis. If the cross sections of <i>S</i> perpendicular to the <i>x</i> —axis are squares, then the volume of <i>S</i> is <b>(Calculator)</b> (A) $\frac{1}{2}$ (B) $\frac{2}{3}$ (C) 1 (D) 2 (E) $\frac{1}{3}(e^3 - 1)$

9. The area of the region enclosed by the	10. The region enclosed by the $x$ –axis, the
curve $=\frac{1}{1}$ , the x $-$ axis, and the lines x $=$	line $x = 3$ , and the curve $y = \sqrt{x}$ is rotated
3 and $x = 4$ is (Non-Calculator)	about the $x$ —axis. What is the volume of
(A) 5	the solid generated? (Non-Calculator)
$\overline{36}$	(A) $3\pi$
$ln\frac{2}{3}$	(B) $2\sqrt{3\pi}$
(C) $\frac{4}{\ln n}$	$\frac{1}{2}\pi$
(n) 3	(D) $9\pi$
$ln\frac{1}{2}$	$\begin{pmatrix} (E) & \frac{36\sqrt{3}}{\pi} \pi \end{pmatrix}$
(E) <i>ln</i> 6	5
11. What is the average value of y for the	12. The volume of the solid obtained by
part of the curve $y = 3x - x^2$ which is in the	revolving the region enclosed by the ellipse
first quadrant ? (Non-Calculator)	$x^2 + 9y^2 = 9$ about the $x$ –axis is
(A) $-6$	(Non-Calculator)
(B) $-2$ (C) 3	(A) $2\pi$
	$\begin{array}{c} (B) & 4\pi \\ (C) & 6\pi \end{array}$
(D) $\frac{9}{4}$	(D) $9\pi$
(E) <sup>9</sup>	(E) $12\pi$
$\frac{\overline{2}}{12}$	
13. The area of the region in the <u>first</u>	14. The average value of $f(x) = x^2 \sqrt{x^3 + 1}$
$\frac{\text{quadrant}}{\text{quadrant}}$ that is enclosed by the graphs of $y = y^3 + 0$ and $y = y + 0$ is (Non	on the closed interval [0,2] is(Non-
$y = x^2 + 8$ and $y = x + 8$ is (NOR-	Calculator)
(A)  1	$\left( \begin{array}{c} (A) \\ \hline 9 \end{array} \right)$
4	(B) $\frac{13}{1}$
(B) $\frac{1}{2}$	$\begin{pmatrix} 3 \\ (C) & 26 \end{pmatrix}$
(C) $\frac{2}{3}$	
	(D) 13 (F) 26
(D) 1 (F) 65	(E) 20
<u> </u>	
15. The area of the region bounded by the	16. The area of the region enclosed by the
lines $x = 0$ , $x = 2$ , and $y = 0$ and the curve	graphs of $y = x$ and $y = x^2 - 3x + 3$ is
$y = e^{\frac{2}{2}}$ is (Calculator)	(Calculator)
(A) $e - 1$	(A) $\frac{2}{3}$
(B) $e - 1$	(B) 1
(C) $2(e-1)$	(C) $\frac{4}{2}$
(D) $2e - 1$	$\begin{vmatrix} 3\\ D \end{vmatrix}$
(E) <i>2e</i>	(E) <u>14</u>
	3

1.B 2.C 3.B 4.D 5.A 6.E 7.C 8.C 9.D 10.C 11.C 12.B 13.A 14.A 15.C 16.C