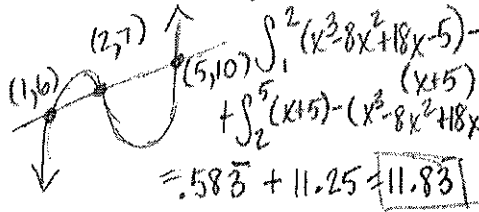


1. What is the area enclosed by the curves $y = x^3 - 8x^2 + 18x - 5$ and $y = x + 5$?

(Calculator)

- (A) 10.667
- (B) 11.833
- (C) 14.583
- (D) 21.333
- (E) 32



2. What is the average value of $y = \frac{\cos x}{x^2 + x + 2}$ on the closed interval $[-1, 3]$? (Calculator)

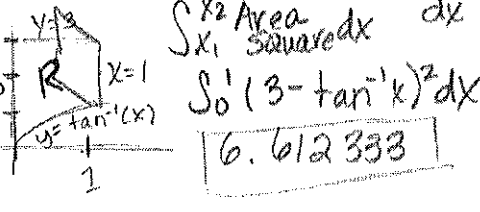
- (A) -0.085
- (B) 0.090
- (C) 0.183
- (D) 0.244
- (E) 0.732

$\frac{1}{3-(-1)} \int_{-1}^3 \frac{\cos x}{x^2+x+2} dx$
 $\frac{1}{4} [0.73180422] = 0.18295105$

3. The base of a solid is the region in the first quadrant bounded by the y -axis, the graph of $y = \tan^{-1} x$, the horizontal line $y = 3$, and the vertical line $x = 1$. For this solid, each cross section perpendicular to the x -axis is a square. What is the volume of the solid?

(Calculator)

- (A) 2.561
- (B) 6.612
- (C) 8.046
- (D) 8.755
- (E) 20.773



4. If $0 \leq k < \frac{\pi}{2}$ and the area under the curve $y = \cos x$ from $x = k$ to $x = \frac{\pi}{2}$ is 0.1, then

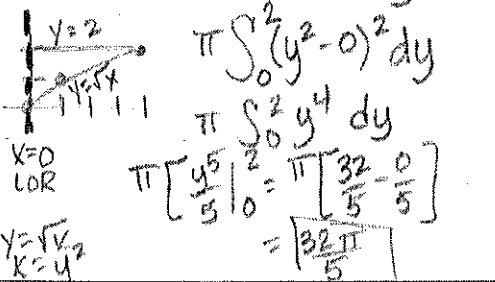
$k =$

- (A) 1.471
- (B) 1.414
- (C) 1.277
- (D) 1.120
- (E) 0.436

(Calculator)
 $\int_k^{\pi/2} \cos x dx = 0.1$
 $\sin x \Big|_k^{\pi/2} = 0.1$
 $\sin(\pi/2) - \sin k = 0.1$
 $1 - \sin k = 0.1$
 $\sin k = 0.9$
 $k = \sin^{-1}(0.9) = 1.119769515$

5. If the region enclosed by the y -axis, the line $y = 2$, and the curve $y = \sqrt{x}$ is revolved about the y -axis, the volume of the solid generated is

- (A) $\frac{32\pi}{5}$
- (B) $\frac{16\pi}{3}$
- (C) $\frac{3}{16\pi}$
- (D) $\frac{5}{8\pi}$
- (E) $\frac{3}{\pi}$



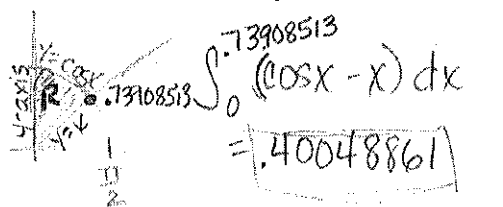
6. The average value of $\cos x$ on the interval $[-3, 5]$ is

- (A) $\frac{\sin 5 - \sin 3}{8}$
- (B) $\frac{\sin 5 - \sin 3}{5 - 3}$
- (C) $\frac{\sin 3 - \sin 5}{8}$
- (D) $\frac{\sin 3 + \sin 5}{8}$
- (E) $\frac{\sin 3 + \sin 5}{8}$

(Non-Calculator)
 $\frac{1}{5-(-3)} \int_{-3}^5 \cos x dx$
 $\frac{1}{8} [\sin x]_{-3}^5$
 $\frac{1}{8} (\sin 5 - \sin(-3))$
 $\frac{1}{8} (\sin 5 + \sin 3)$

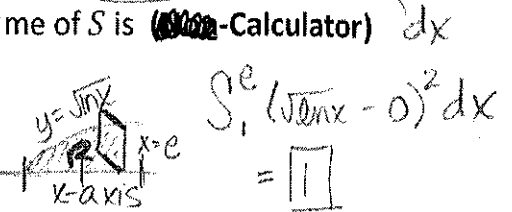
7. What is the area of the region in the first quadrant enclosed by the graphs of $y = \cos x$, $y = x$, and the y -axis?

- (A) 0.127
- (B) 0.385
- (C) 0.400
- (D) 0.600
- (E) 0.947



8. The base of a solid S is the region enclosed by the graph of $y = \sqrt{\ln x}$, the line $x = e$, and the x -axis. If the cross sections of S perpendicular to the x -axis are squares, then the volume of S is

- (A) $\frac{1}{2}$
- (B) $\frac{2}{3}$
- (C) 1
- (D) 2
- (E) $\frac{1}{3}(e^3 - 1)$



9. The area of the region enclosed by the curve $y = \frac{1}{x-1}$, the x -axis, and the lines $x = 3$ and $x = 4$ is (Non-Calculator)

- (A) $\frac{5}{36}$
- (B) $\ln \frac{2}{3}$
- (C) $\ln \frac{4}{3}$
- (D) $\ln \frac{3}{2}$
- (E) $\ln 6$

$\int_3^4 \frac{1}{x-1} dx$ $u=x-1$
 $du = dx$
 $u(3)=2$
 $u(4)=3$
 $\int_2^3 \frac{1}{u} du$
 $\ln u \Big|_2^3 = \ln 3 - \ln 2 = \ln \frac{3}{2}$

10. The region enclosed by the x -axis, the line $x = 3$, and the curve $y = \sqrt{x}$ is rotated about the x -axis. What is the volume of the solid generated? (Non-Calculator)

- (A) 3π
- (B) $2\sqrt{3}\pi$
- (C) $\frac{9}{2}\pi$
- (D) 9π
- (E) $\frac{36\sqrt{3}}{5}\pi$

$\pi \int_0^3 (\sqrt{x}-0)^2 dx$
 $\pi \int_0^3 x dx$
 $\pi \left[\frac{x^2}{2} \right]_0^3$
 $\pi \left[\frac{9}{2} - 0 \right] = \frac{9\pi}{2}$

11. What is the average value of y for the part of the curve $y = 3x - x^2$ which is in the first quadrant? (Non-Calculator)

- (A) -6
- (B) -2
- (C) $\frac{3}{2}$
- (D) $\frac{4}{9}$
- (E) $\frac{9}{2}$

$\frac{1}{3-0} \int_0^3 (3x-x^2) dx$
 $\frac{1}{3} \left[\frac{3x^2}{2} - \frac{x^3}{3} \right]_0^3$
 $\frac{1}{3} \left[\frac{27}{2} - \frac{27}{3} \right] = \frac{1}{3} \left[\frac{27}{2} - 9 \right] = \frac{1}{3} \left[\frac{27}{2} - \frac{18}{2} \right] = \frac{1}{3} \left[\frac{9}{2} \right] = \frac{3}{2}$

12. The volume of the solid obtained by revolving the region enclosed by the ellipse $x^2 + 9y^2 = 9$ about the x -axis is (Non-Calculator)

- (A) 2π
- (B) 4π
- (C) 6π
- (D) 9π
- (E) 12π

$\pi \int_{-3}^3 (\sqrt{9-x^2})^2 dx$
 $\pi \int_{-3}^3 (9-x^2) dx$
 $\pi \left[9x - \frac{x^3}{3} \right]_{-3}^3$
 $\pi \left[27 - 9 - (-27 + 9) \right] = \pi [18 - (-18)] = 36\pi$

13. The area of the region in the first quadrant that is enclosed by the graphs of $y = x^3 + 8$ and $y = x + 8$ is (Non-Calculator)

- (A) $\frac{1}{4}$
- (B) $\frac{1}{3}$
- (C) $\frac{2}{3}$
- (D) $\frac{4}{3}$
- (E) $\frac{65}{4}$

$\int_0^1 (x+8) - (x^3+8) dx$
 $\int_0^1 (x - x^3) dx$
 $\left[\frac{x^2}{2} - \frac{x^4}{4} \right]_0^1$
 $\left(\frac{1}{2} - \frac{1}{4} \right) - (0) = \frac{1}{4}$

14. The average value of $f(x) = x^2\sqrt{x^3+1}$ on the closed interval $[0,2]$ is (Non-Calculator)

- (A) $\frac{26}{9}$
- (B) $\frac{13}{3}$
- (C) $\frac{26}{3}$
- (D) $\frac{13}{3}$
- (E) $\frac{26}{9}$

$\frac{1}{2-0} \int_0^2 x^2 \sqrt{x^3+1} dx$
 $\frac{1}{6} \int_1^9 u^{1/2} du$
 $\frac{1}{6} \left[\frac{2}{3} u^{3/2} \right]_1^9 = \frac{1}{9} \left[(27) - (1) \right] = \frac{26}{9}$

15. The area of the region bounded by the lines $x = 0$, $x = 2$, and $y = 0$ and the curve $y = e^{x/2}$ is (Non-Calculator)

- (A) $\frac{e-1}{2}$
- (B) $e-1$
- (C) $2(e-1)$
- (D) $2e-1$
- (E) $2e$

$\int_0^2 (e^{x/2} - 0) dx$
 $2 \int_0^1 e^u du$
 $2e^u \Big|_0^1 = 2e - 2$

16. The area of the region enclosed by the graphs of $y = x$ and $y = x^2 - 3x + 3$ is (Calculator)

- (A) $\frac{2}{3}$
- (B) $\frac{1}{3}$
- (C) $\frac{4}{3}$
- (D) $\frac{2}{3}$
- (E) $\frac{14}{3}$

$\int_0^3 (x - (x^2 - 3x + 3)) dx$
 $\int_0^3 (4x - x^2 - 3) dx$
 $\left[2x^2 - \frac{x^3}{3} - 3x \right]_0^3$
 $\left(18 - 9 - 9 \right) - (0 - 0) = 0$