

Homework

Name Guide Pd.

Additional Differential Equations Day 2

BC Calculus

Differential Equations

Do these problems **without** a calculator.

1. Use Euler's method with step size 0.5 to compute the approximate y-values $y_1, y_2, y_3,$ and y_4 of the solution of the initial-value problem $y' = xy - x^2, y(1) = 0$.

X	$\Delta x \cdot y'$	y
1	$\frac{1}{2}[xy - x^2]$	0
1.5	$\frac{1}{2}[(1)(0) - (1)^2] = \frac{1}{2}(-1) = -\frac{1}{2}$	$0 - \frac{1}{2}$ -1/2
2	$\frac{1}{2}[\frac{3}{2}(-\frac{1}{2}) - (\frac{3}{2})^2] = \frac{1}{2}[\frac{-12}{4}] = -\frac{3}{2}$	$-\frac{1}{2} - \frac{3}{2}$ -2
2.5	$\frac{1}{2}[2(-2) - (2)^2] = \frac{1}{2}[-8] = -4$	$-2 - 4$ -6
3	$\frac{1}{2}[\frac{5}{2}(-6) - (\frac{5}{2})^2] = \frac{1}{2}[\frac{-85}{4}] = -10.625$	$-6 - 10.625$ -16.625

2. Use Euler's method with step size 0.2 to estimate $y(0.4)$, where $y(x)$ is the solution of the initial-value problem $y' = x + y^2, y(0) = 0$.

Do these problems **with** a calculator and check with a calculator

3. Use Euler's method with step size 0.2 to estimate $y(1)$, where $y(x)$ is the solution of the initial-value problem $y' = xy - x^2, y(0) = 1$.

X	$\Delta x \cdot y'$	y
0	$(.2)[xy - x^2]$	1
.2	$(.2)[0(1) - (0)^2] = 0$	$1 + 0$ 1
.4	$(.2)[(.2)(1) - (.2)^2] = .032$	$1 + .032$ 1.032
.6	$(.2)[(.4)(1.032) - (.4)^2] = .05056$	$1.032 + .05056$ 1.08256
.8	$(.2)[(.6)(1.08256) - (.6)^2] = .0579072$	$1.08256 + .0579072$ 1.140467
1	$(.2)[(.8)(1.140467) - (.8)^2] = .054474$	$1.140467 + .054474$ 1.1949

4. Use Euler's method with step size 0.1 to estimate $y(0.5)$, where $y(x)$ is the solution of the initial-value problem $y' = y + xy, y(0) = 1$.

5. **Calculator** Use Euler's method with step size 0.1 to estimate $y(0.4)$, where $y(x)$ is the solution of the initial-value problem $y' = x + y^2$, $y(0) = 0$.

6. **Non-Calculator** Use Euler's method with step size 0.5 to estimate $y(2)$, where $y(x)$ is the solution of the initial-value problem $y' = xy - x$, $y(0) = 1$.

7. Use Euler's method with step size 0.5 to estimate $y(2)$ where $y(x)$ is the solution to the initial value problem $y' = x(y - x)$, $y(1) = 2$

- a. 2.125 b. 2 c. 3 d. 2.75 e. 3.25

Review

R1. If $f(x) = x + \sin x$, then $f'(x) =$

- a. $1 + \cos x$ b. $1 - \cos x$ c. $\cos x$ d. $\sin x - x \cos x$ e. $\sin x + x \cos x$

R2. If $y = \cos^2(3x)$, then $\frac{dy}{dx} =$

$y = [\cos(3x)]^2$
Rewrite & use chain rule 2 times

- a. $-6 \sin 3x \cos 3x$ b. $-2 \cos 3x$ c. $2 \cos 3x$ d. $6 \cos 3x$ e. $2 \sin 3x \cos 3x$

R3. If $y = \cos^2 x - \sin^2 x$, then $y' =$

$y = [\cos x]^2 - [\sin x]^2$ Remember $\sin(2x) = 2 \sin x \cdot \cos x$

- a. -1 b. 0 c. $-2 \sin 2x$ d. $-2(\cos x + \sin x)$ e. $2(\cos x - \sin x)$

Answers

- | | | |
|--------------------------------------------------------|----------------------------|-------|
| 1. $y_1 = -0.5, y_2 = -2$
$y_3 = -6, y_4 = -16.625$ | 4. $y(0.5) \approx 1.7616$ | 7. C |
| 2. $y(0.4) \approx 0.04$ | 5. $y(0.4) \approx 0.0601$ | R1. A |
| 3. $y(1) \approx 1.1949$ | 6. $y(2) \approx 1$ | R2. A |
| | | R3. C |