

$t$	0	25	30	45	65	80
$W(t)$	2	10	13	30	60	81

**BC1:** Workers at a local office building are expected to be at work by 9AM ( $t = 60$ ) each day.

Let the twice differentiable function  $y = W(t)$  be the amount of workers in the building at

time  $t$ , in minutes, satisfying the logistic differential equation  $\frac{dy}{dt} = \frac{1}{15}y\left(1 - \frac{y}{100}\right)$

where  $W(0) = 2$ . Selected values of  $W(t)$  are given in the table where  $t = 0$  is 8AM.

(a) Find  $W'(65)$  and  $W''(65)$ . Using correct units, interpret the meaning of  $W''(65)$  in context of this problem.

(b) Evaluate  $\int_0^{\infty} W'(3t + 25)dt$ . Show the work that leads to your answer.

(c) Use a left Riemann sum with three subintervals indicated by the data in the table to approximate the value of  $\frac{1}{45} \int_0^{45} W(t)dt$ . Using correct units, explain the meaning of  $\frac{1}{45} \int_0^{45} W(t)dt$  in the context of the problem.

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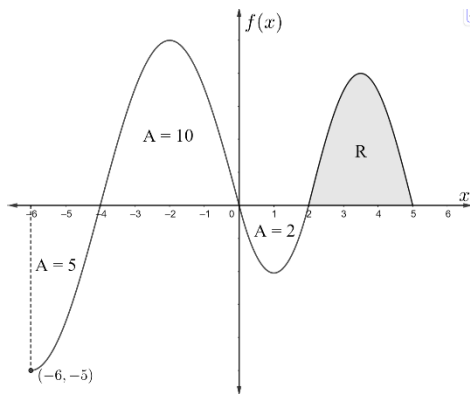
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where  $W(0) = 2$ . Selected values of  $W(t)$  are given in the table where  $t = 0$  is 8AM.

(d) Use Euler's method with two steps of equal size starting at  $t = 45$  minutes to approximate the number of workers inside the office building by 9:25AM ( $t = 85$  minutes).

(e) Is there a time  $c$ , such that  $25 < c < 45$ , when  $W'(c) = 1$ . Justify your answer.

(f) Let  $P_2(t)$  be the second degree Taylor polynomial for  $W(t)$  centered at  $t = 65$ . Find  $P_2(t)$  and use it to approximate the number of workers inside the office building at 9:25AM ( $t = 85$ ).



**BC2:** The function  $f$  is twice differentiable for  $x \geq -6$ . A portion of the graph of  $f$  is given in the figure above. The areas formed by the bounded regions between the graph of  $f$  and the  $x$  axis are labeled in the figure. Let the twice differentiable function  $g$  be defined by  $g(x) = \int_2^x f(t) dt$ .

(a) Find  $\lim_{x \rightarrow -2} \frac{g(2x) - 4x}{e^{x^2-4} + x - 1}$ .

(b) Find the absolute maximum of  $g$  on the interval  $[-6, 2]$ . Justify your answer.

(c) Evaluate  $\int_{-3}^1 x f'(2x) dx$ .

(d) The region R is the base of a solid whose cross sections perpendicular to the  $x$  axis are squares. Write, but do not evaluate, an integral expression that gives the volume of the solid.

(e) For  $x \geq 5$ , the function  $f$  is not explicitly given, but  $f'(x) = -4 \left(\frac{1}{2}\right)^{x-5}$ . If  $a_n = f'(n)$ ,

find  $\sum_{n=5}^{\infty} a_n$  or show that the series diverges.